

introduction

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Sci.supervisors:

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Sci.interests:

regularization

of inverse problems



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regularized fixed-point

$$\hat{u}: \quad Fu = y$$



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regularized fixed-point

$$\hat{u}: \quad Fu = y \quad F = A + G$$



regularized fixed-point

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$Au = y - Gu$$



regularized fixed-point

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$Au_{k+1} = y - Gu_k$$



regularized fixed-point

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$Au_{k+1} = y_\delta - Gu_k$$



regularized fixed-point

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$A^* Au_{k+1} = A^*(y - Gu_k)$$



regularized fixed-point

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$u_{k+1} = (A^*A)^\dagger A^*(y - Gu_k)$$



regularized fixed-point

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$u_{k+1} = (A^* A)^\dagger A^* (y - Gu_k)$$

$$u_{k+1}^\alpha = g_\alpha (A^* A) A^* (y_\delta - Gu_k)$$



regularized fixed-point

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$u_{k+1} = (A^* A)^\dagger A^* (y - Gu_k)$$

$$u_{k+1}^\alpha = g_\alpha(A^* A) A^* (y_\delta - Gu_k)$$

$$\|\hat{u} - u_{k+1}^\alpha\| \leq \varphi(\alpha) + \frac{\delta}{\lambda(\alpha)} + \rho \|\hat{u} - u_k\|$$



balancing principle

$$\|\hat{u} - u^\alpha\| \leq \varphi(\alpha) + \frac{\delta}{\lambda(\alpha)}$$

$$\Delta = \{\alpha_i, i = 1, \dots, N\}$$



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$$i_{\text{opt}} = \max \left\{ i \mid \|u^{\alpha_i} - u^{\alpha_j}\| \leq \frac{4\delta}{\lambda(\alpha_j)}, j = 1, \dots, (i-1) \right\}$$



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$$\|\hat{u} - u^{\alpha_{i_{\text{opt}}}}\| \leq b(\delta)$$



balancing principle

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balancing principle

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Hui Cao

RICAM,

Group Inverse Problems



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